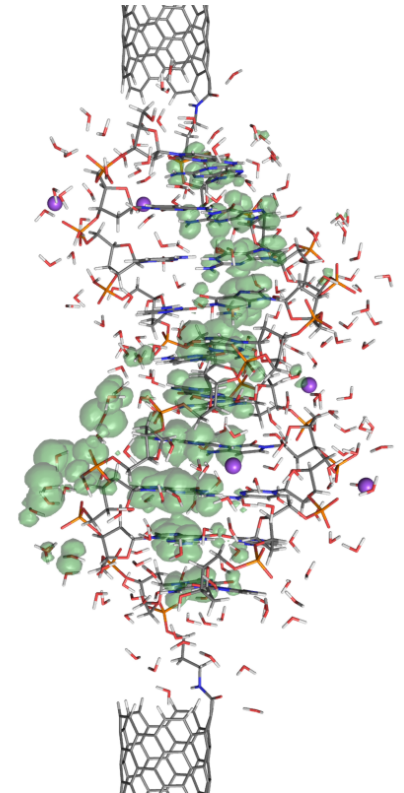


Petascale Quantum Simulations of Nano Systems and Biomolecules

Emil Briggs
North Carolina State University

1. Outline of real-space Multigrid (RMG)
2. Scalability and hybrid/threaded models
3. GPU acceleration
4. RmgLib
5. Application: Electron transport in DNA
Conduction mechanisms
Counterions, water, base pair matching

Collaborators: Wenchang Lu, Bikan Tan, Yan Li,
Miroslav Hodak, Jerzy Bernholc



Real-space Multi-Grid (RMG)

- Density functional equations solved directly on the grid instead of with plane waves
- Multigrid techniques remove instabilities by working on one length scale at a time
- Convergence acceleration and automatic preconditioning on all length scales
- Non-periodic boundary conditions are as easy as periodic
- Compact “Mehrstellen” discretization

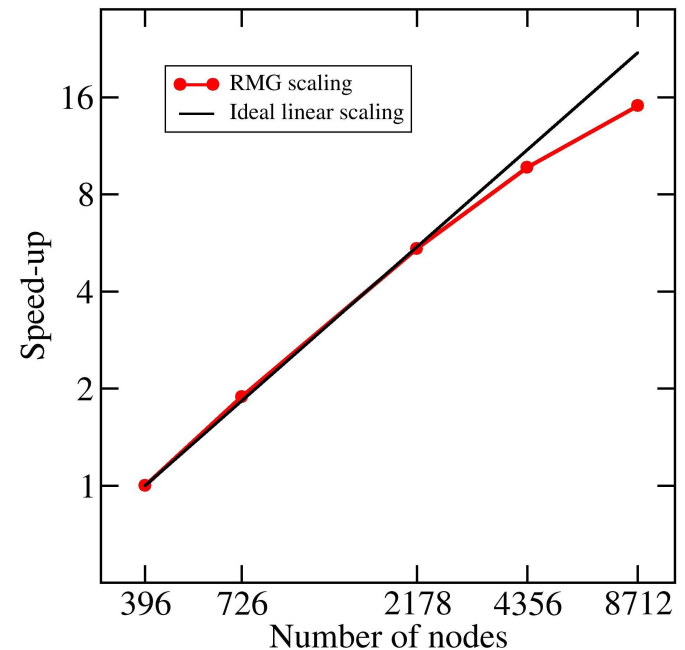
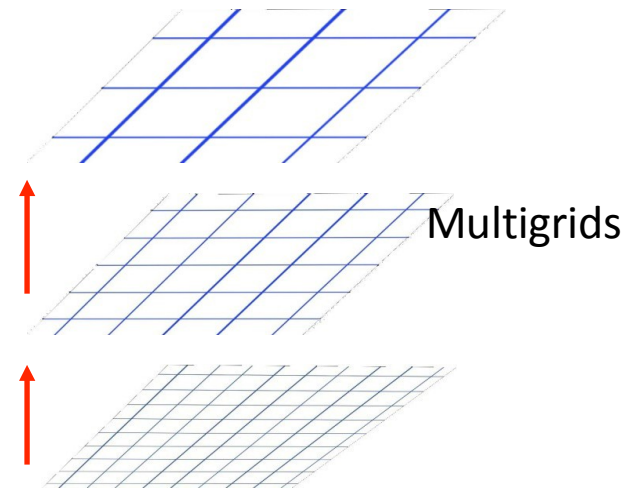
$$A[\phi_i] + B[(V_{eff} + V_{NL})\phi_i] = \epsilon_i B[S\phi_i]$$

- Allows for efficient massively parallel implementation (no FFTs)

See E. L. Briggs, D. J. Sullivan and J. Bernholc
Phys. Rev. B 54, 14362 (96).

Ultrasoft pseudopotentials:

M. Hodak, S. Wang, W. Lu and J. Bernholc,
PRB 76, 085108 (07)



Scalability as HPC architecture changes

Multisocket/multicore SMP nodes

1999 – Cray T3E 1-socket and core per node

2013 – Cray XK6 2-sockets and 32 cores per node

2020 - ?

High speed interconnect between nodes

Infiniband

Myrinet

Cray Gemini

GPU/Accelerator

Nvidia Fermi/Tesla/Kepler

AMD Radeon HD

Intel Xeon PHI

Current machines **400,000** cores

Next generation **1,000,000** cores

Schematic of Cray XE6

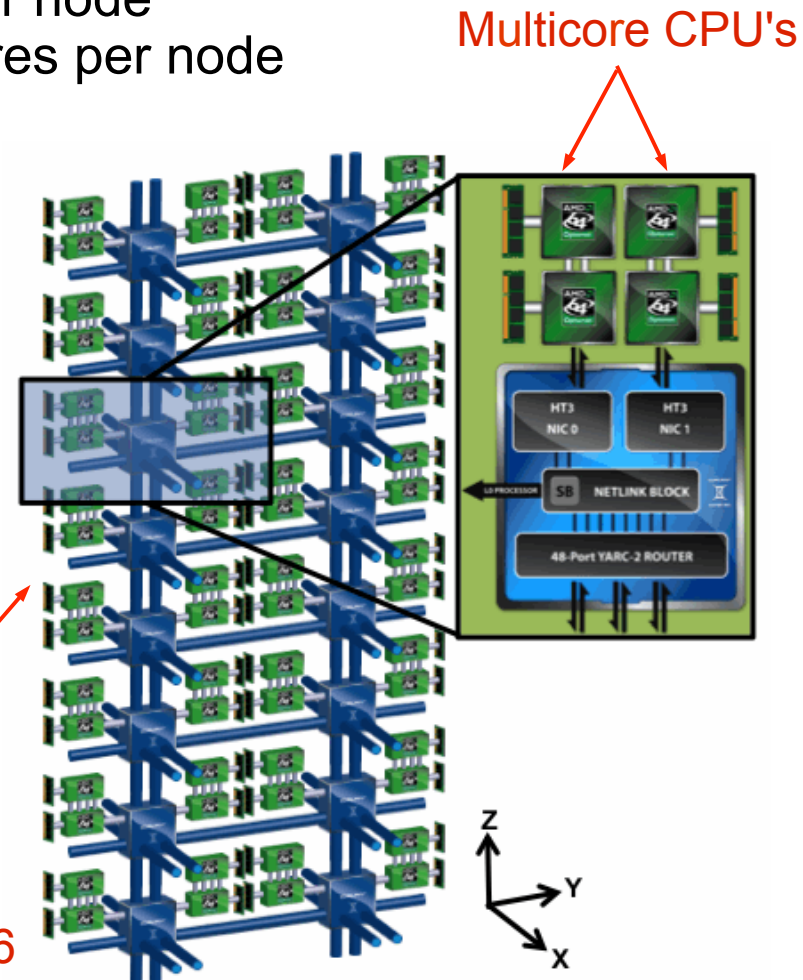


Image courtesy of Cray, Inc.

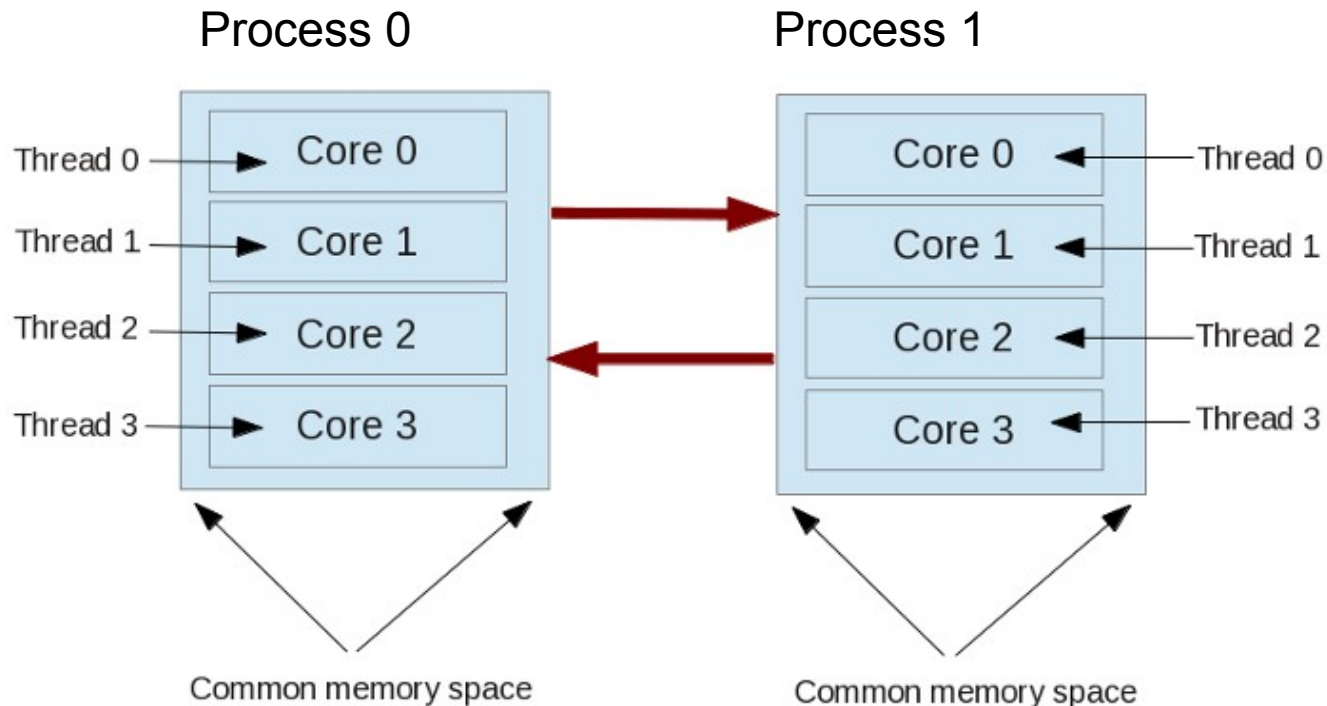
Hybrid MPI/threads/OpenMP to improve scalability

Use 1 MPI process per node rather than 1 process per core

Inter node parallelization uses traditional MPI

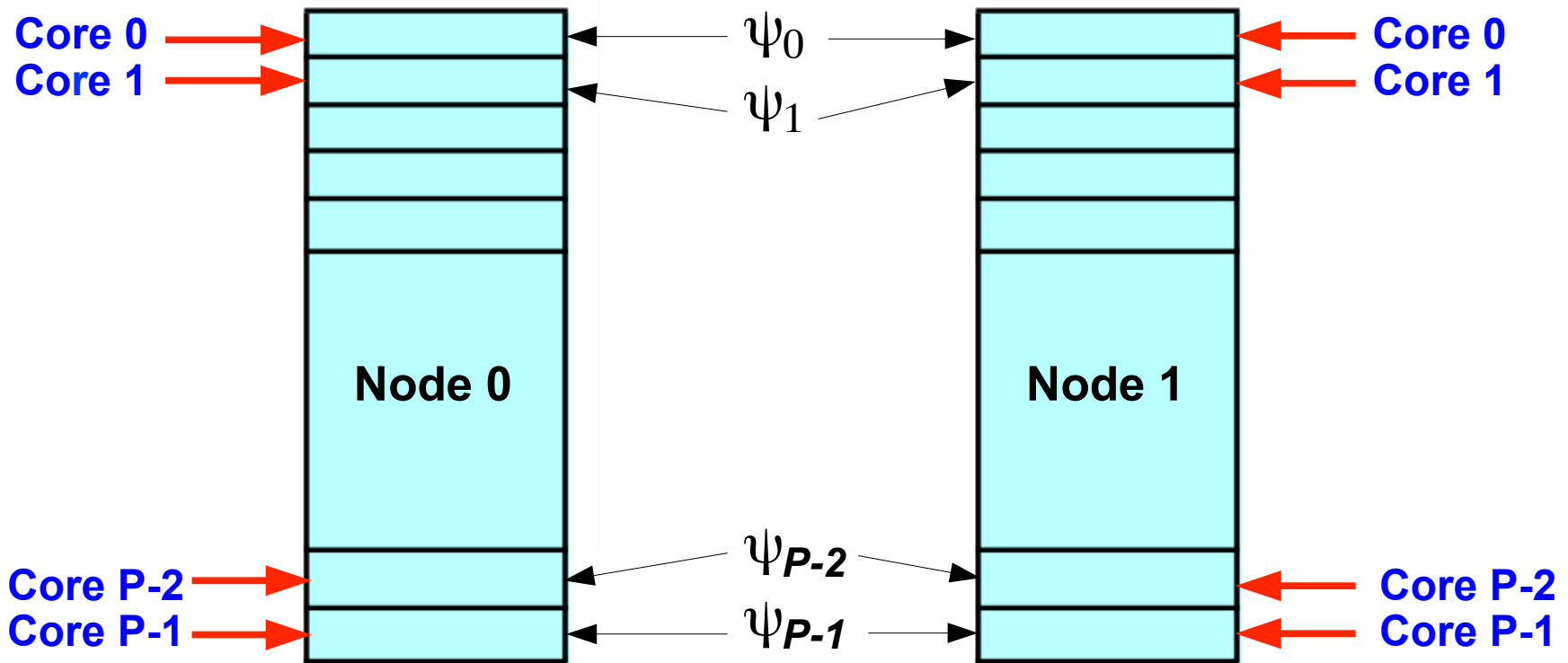
Intra node parallelization uses shared memory threads

Extra cores used via Libraries, Pthreads, Openmp



Pthreads for multigrid preconditioner

Consider a typical electronic structure problem with N orbitals
The computer system used for solution has P processing cores per node
Orbitals may be processed independently and $N \gg P$
Natural parallelization method is to assign each orbital to a single core
OpenMP or Pthreads should work equally well

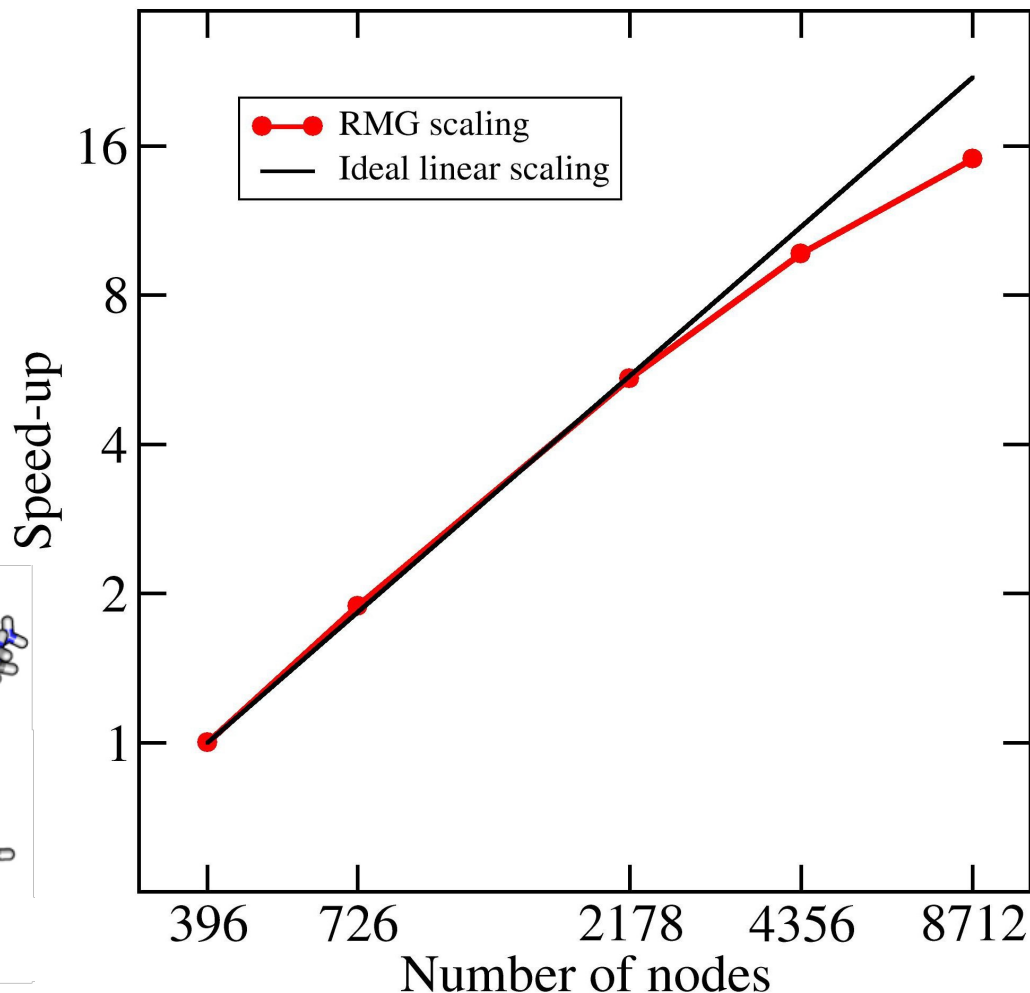
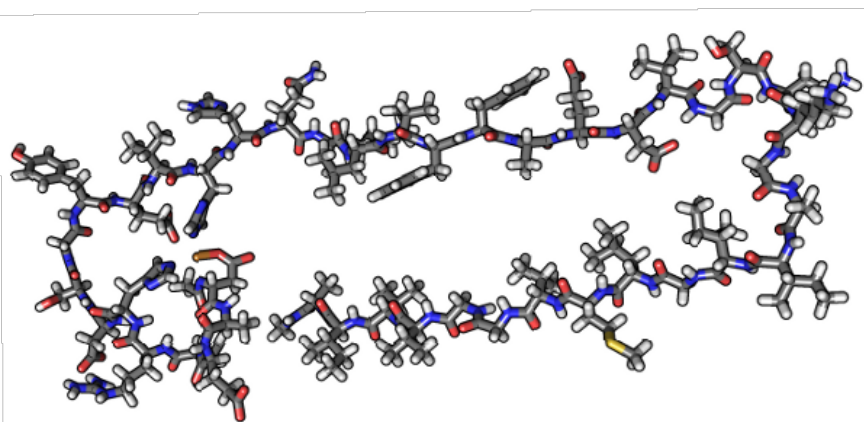


While each thread can operate independently is this the best approach?

Scaling test

Test problem: Gas phase Amyloid
Beta 1-42 protein
Test system: Cray XK7
1 node = 16 Opeteron cores + 1
Nvidia K20x GPU accelerator
Strong scaling

Largest run used **139,392** CPU
cores and **8712** GPU's.



Each node has 16 cores

GPU acceleration for RMG

GPU programming very different from CPU

CPU:

High clock speed, small number of powerful execution units.
Memory latency hidden by caches and out of order execution.
Good single-threaded performance.

GPU:

Low clock speed, large number of weaker execution units.
Memory latency hidden by high thread counts.
Poor single-threaded performance.

Most HPC codes have components that only run well on CPU's

Mixed CPU/GPU model required
Data transfer issues from CPU to GPU (PCI bus latency)

Hints: **Avoid writing GPU code as much as possible.**
Use vendor supplied libraries.
Data transfer issues still require careful consideration

GPU performance improvements

Small test case: C60 molecule in vacuum

60 atoms: 200 electronic orbitals

CPU only calculation Xeon

workstation: 12 cores No

GPU's

10.32 seconds/SCF step

CPU/GPU calculation

Xeon workstation: 12 cores

1 Nvidia K20 GPU

6.72 seconds/SCF step

Speedup of approximately 1.53

Large test case: Solvated amyloid beta protein fragment

3337 atoms: 4672 electronic orbitals

CPU only calculation

2904 nodes: 92,928 Opteron cores

No GPU's

76 seconds/SCF step

CPU/GPU calculation

2904 nodes: 46,464 Opteron cores

2904 Nvidia K20x GPU's

25 seconds/SCF step

Speedup of approximately 3.02

Performance on 3,872 Cray XK7 (K20x GPU) Blue Water nodes: **1.14 PFLOPS**

Introducing RmgLib

Portable library of C++ routines for HPC including

- Grid decomposition across MPI nodes

- Threading on a node

- Finite differencing (Mehrstellen and central operators)

- Communications (asynchronous ghost images)

- Recursive Multigrid solver with support routines

Library supports multiple data types including

- Float, double, complex

Linux/Unix, Windows and OS/X support

- Cmake build system

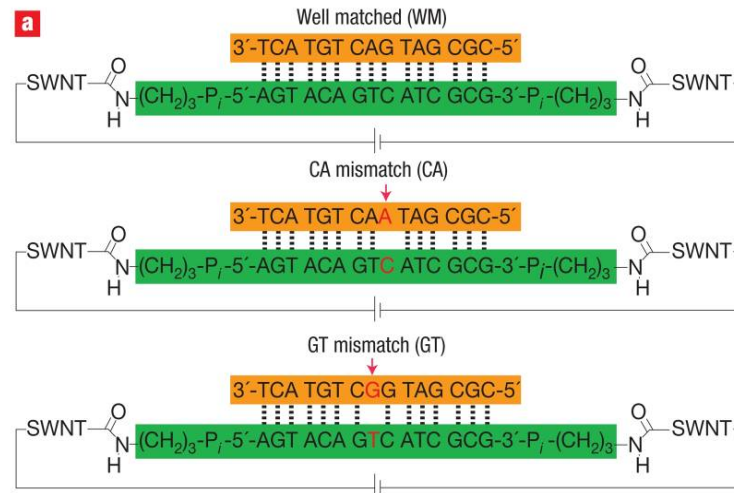
Open source (BSD type) licensing with initial release in 2nd half 2014

Single DNA Electron Transport

Guo, Barton, Nuckolls et al. *Nature Nanotechnol.* 2008

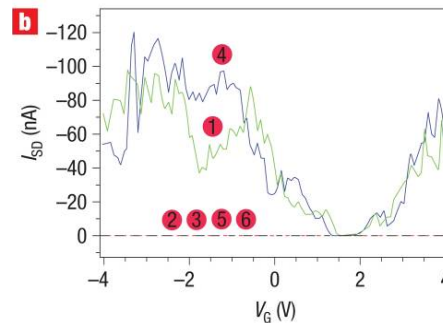
- Experiment in 0.05 mol/L saline solution
- Single walled carbon nanotubes as leads
- Alkane linkers $-\text{CONH}-(\text{CH}_2)_3$ connect B-form DNA to leads
- Very high transmission ($T=0.05$) gives resistance around 0.5 M Ω
- A single GT or AC mismatch increases the resistance of DNA nearly 300-fold relative to a well-matched one

G-guanine; C-cytosine; A-adenine; T-thymine

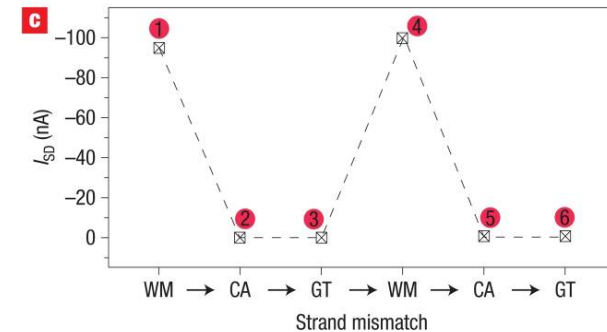


Our goals are to investigate the effects of

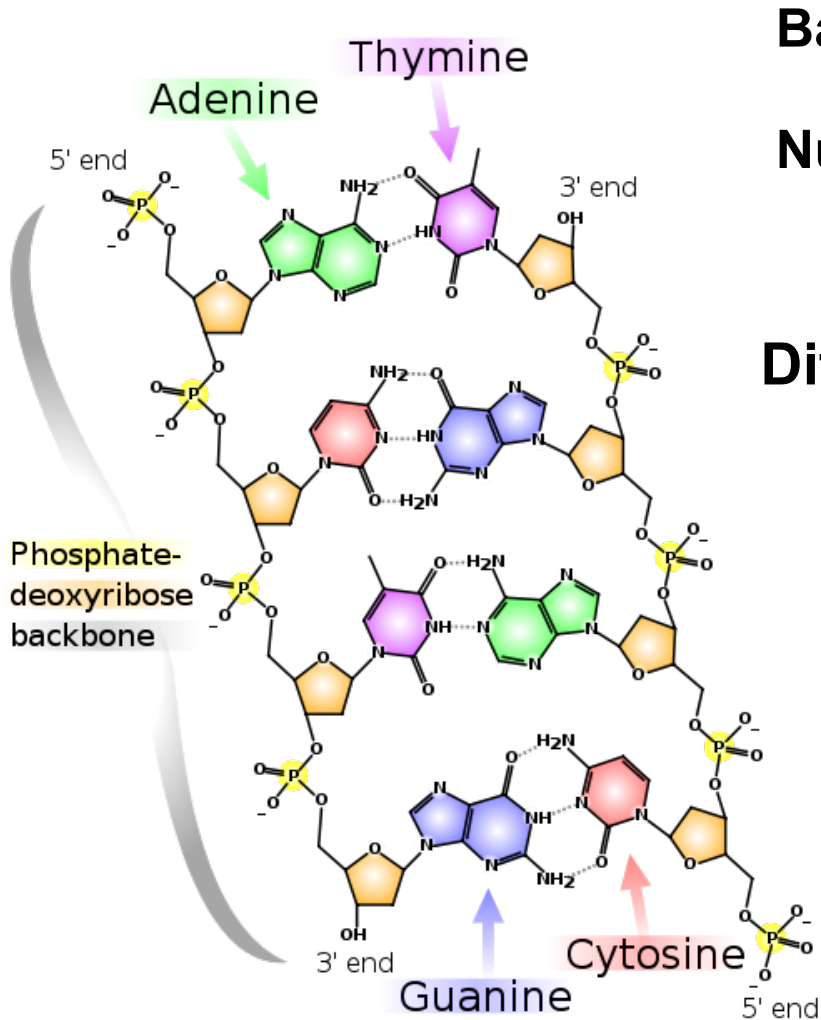
- Linkers
- Counterions
- Solvent
- DNA conformation
- DNA sequence



WM ①
CA ②
GT ③
WM ④
CA ⑤
GT ⑥



Introduction to DNA

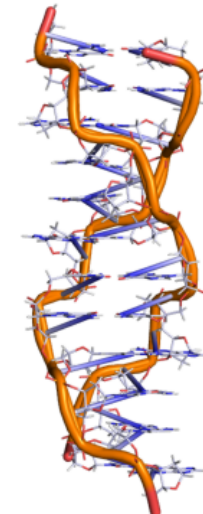
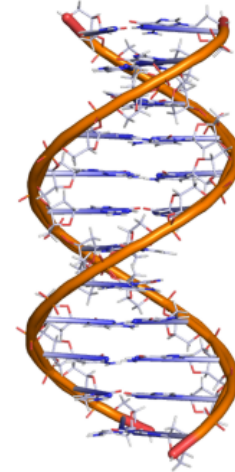
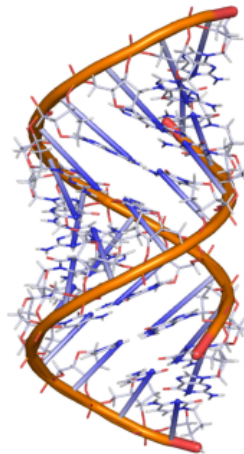


Backbones: sugar rings and phosphate groups

Nucleobases: adenine(A), guanine(G), thymine(T) and cytosine(C). Base pairing can be formed via hydrogen bonds (A-T, G-C)

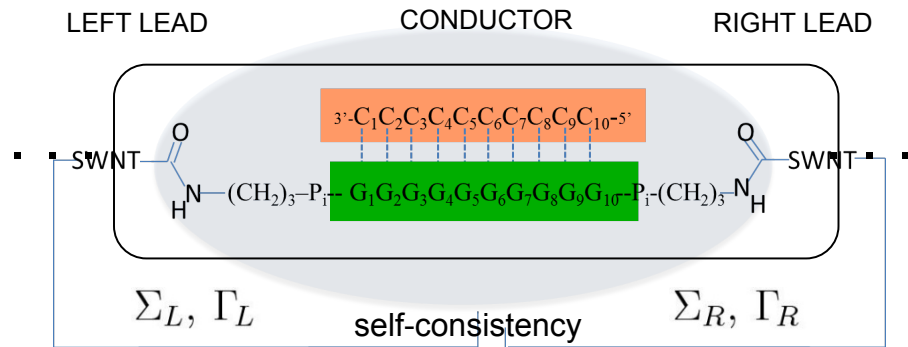
Different forms of DNA:

	A-form	B-form	Z-form
rise:	2.4 Å	3.6 Å	3.7 Å
twist:	33.6°	35.9°	30.0°



Calculations

- 20 snapshots recorded from 2 ns MD simulation for subsequent quantum calculations
- First solvation shell as well as alkane linkers and CNT leads included in the quantum calculation
- $O(N)$ calculation to generate optimized localized orbitals for use in transport calculations
- Iterative non-equilibrium Green function (NEGF) method to calculate transmission self-consistently



Hamiltonian: H_C orbital overlap: S_C

Self-energy: Σ_L Σ_R

$$G_C = (E S_C - H_C - \Sigma_L - \Sigma_R)^{-1}$$

$$T = \text{Tr} \left(\Gamma_L G_C^R \Gamma_R G_C^A \right), \quad \Gamma = \frac{i}{2} (\Sigma^\dagger - \Sigma)$$

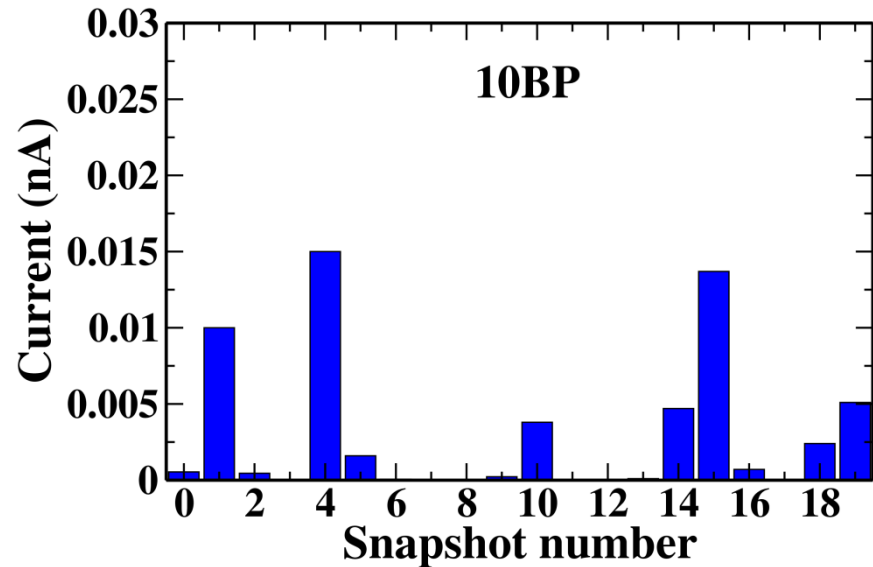
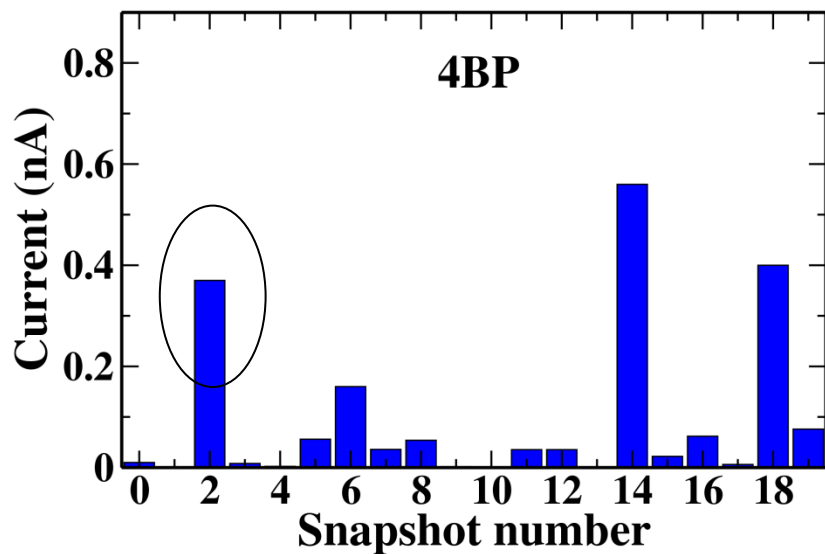
$$I(V) = \frac{2e^2}{h} \int_{-\infty}^{\infty} T(E, V) [f(E - \mu_L) - f(E - \mu_R)] dE$$

Fattebert, Bernholc, Phys. Rev. B 2000

Nardelli, Fattebert, Bernholc, Phys. Rev. B 2001

Lu, Meunier, Bernholc, Phys. Rev. Lett. 2005

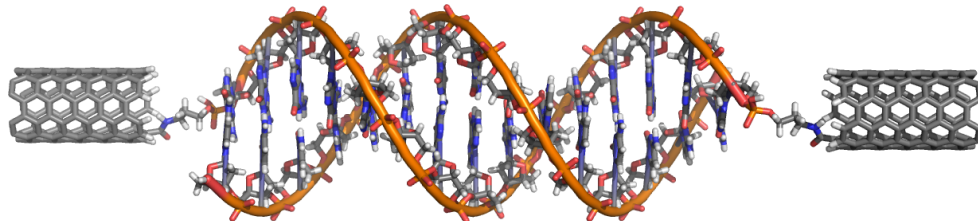
DNA conductivity histogram



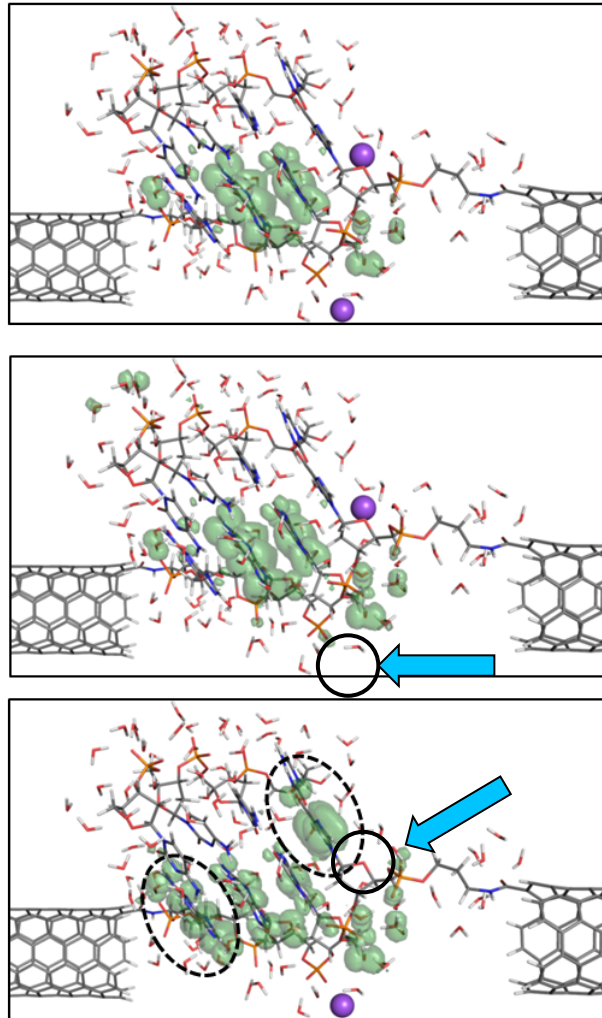
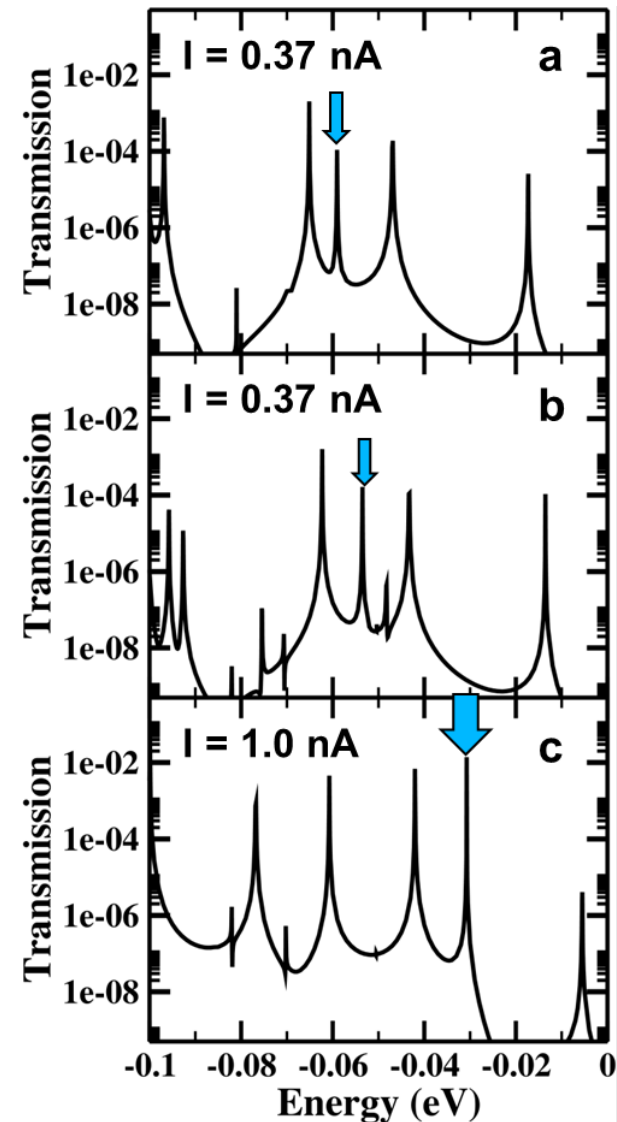
Large variation of conductivity (12 orders of magnitude for 10 BP) among snapshots

- ❖ Conformational gating
- ❖ Average current for 4 BP poly(G)-poly(C) is 0.1 nA
- ❖ Average current for 10 BP poly(G)-poly(C) is 0.0029 nA
- ❖ Assume an exponential decay model:

10 base-pair (10BP)
configuration

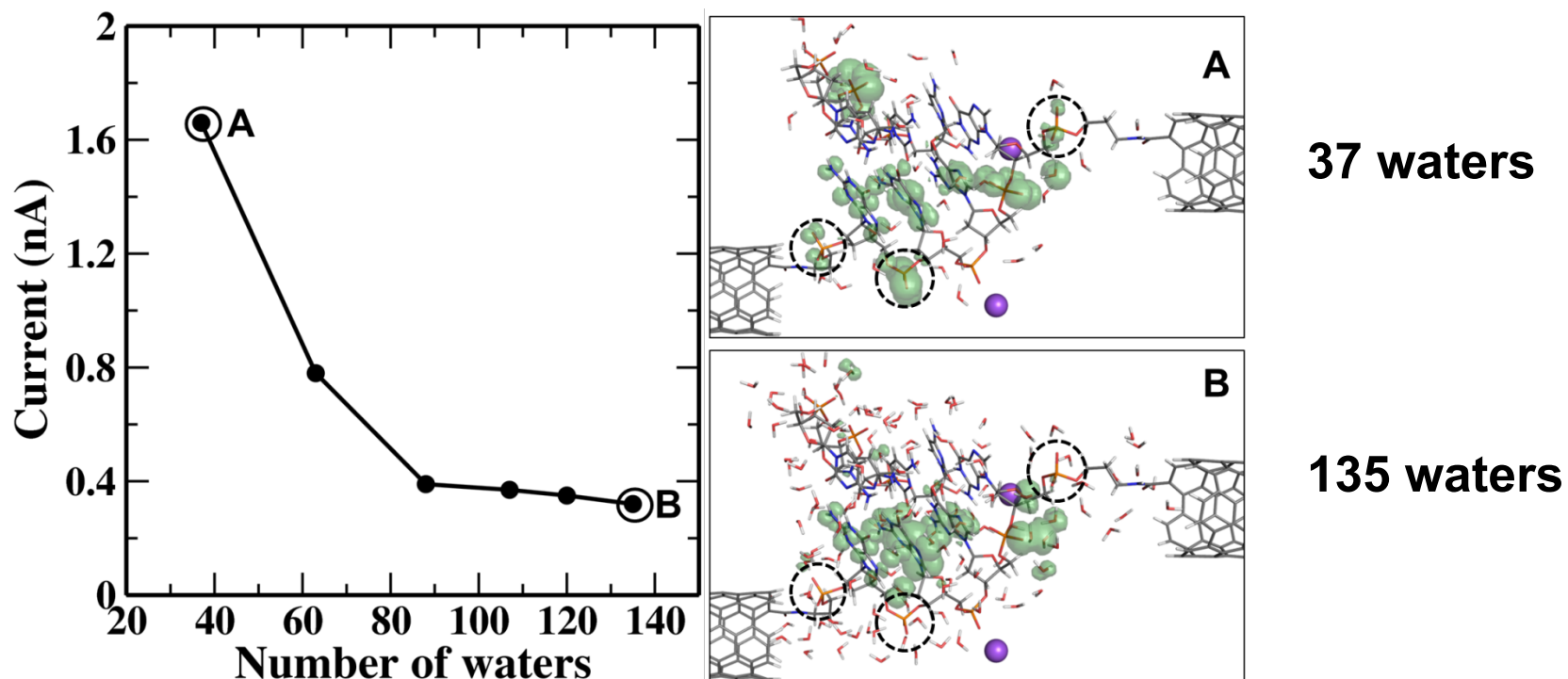


Effect of individual counterions (snapshot 2)



- ❖ Two explicit counterions in snapshot 2 (right panel in a)
- ❖ The conductivity is unchanged when removing the counterion close to the phosphate group
- ❖ After the removal of a counterion near G4, the conductive states become more delocalized and the current increases by a factor of three
- ❖ Average current increases by a factor of 2 after removal of ions for the 20 snapshots

Water effects on DNA conductivity

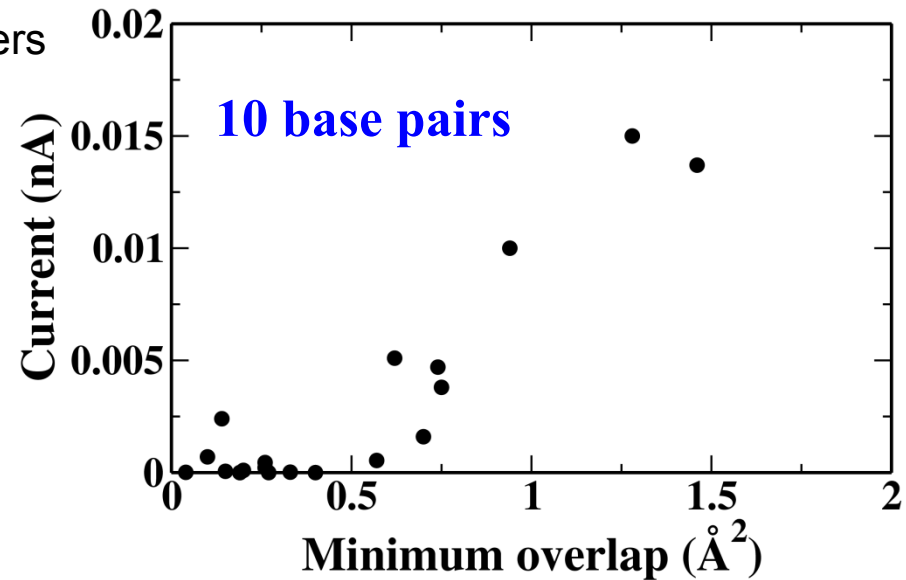


- ❖ Conductivity decreases with the number of water molecules around DNA
- ❖ Water dipoles suppress conducting electrons' amplitude on phosphate groups, leading to reduced conductivity
- ❖ Presence of water decreases the current by a factor of four
- ❖ Presence of ions decreases the current by a factor of two
- ❖ Large variation of conductivity persists

Correlation analysis of 10 BP poly(G)-poly(C) DNA

Correlation of conductivity with helicoidal parameters

	mean	minimum	maximum
twist	0.4888	0.1505	-0.0592
roll	0.1571	-0.0128	0.0126
tilt	0.1303	0.181	0.1959
rise	-0.0833	0.2417	0.1569
slide	0.3821	0.383	-0.1662
shift	0.4568	0.6176	0.1275
overlap	0.4208	0.9106	0.051



- ❖ Helicoidal parameters in DNA calculated using 3DNA
- ❖ We consider correlation of conductivity with not only the mean, but also with minimum and maximum values of the parameters
- ❖ The minimum *overlap* between successive guanine bases has the dominant correlation with conductivity
- ❖ Conductivity is highly sensitive to local distortions
- ❖ Snapshot 15: the minimum overlap is 1.46 \Rightarrow delocalized conducting states with relatively high conductivity (0.0137 nA)
- ❖ Snapshot 15': minimum overlap reduced to 0.73 \Rightarrow less delocalized conducting states and lower conductivity (0.0045 nA)

Summary

❑ RMG code rewrite to enhance scalability and portability

- ❖ Real space multigrid method for electronic structure calculations
- ❖ Hybrid model using MPI/threads/OpenMP
- ❖ GPU acceleration: 1.144 PFLOPS using 3872 Bluewater XK nodes
- ❖ Open source RmgLib to be released in 2nd half 2014

❑ Charge transport in DNA

- ❖ Charge transport through delocalized hole orbitals
- ❖ Highly dependent on instantaneous DNA configuration
- ❖ Largest conductivity for largest *minimum overlap* between guanine bases
- ❖ Counterions and water molecules significantly reduce conductance
- ❖ Unmatched base pairs act as barriers, reduce orbital delocalization.

